# MoULDyS: Monitoring of Autonomous Systems in the Presence of Uncertainties

Bineet Ghosh<sup>a</sup>, Étienne André<sup>b,c</sup>

<sup>a</sup> The University of North Carolina at Chapel Hill, NC, USA <sup>b</sup> Université de Lorraine, CNRS, Inria, LORIA, F-54000 Nancy, France <sup>c</sup> Université Sorbonne Paris Nord, LIPN, CNRS UMR 7030, F-93430 Villetaneuse, France

#### Abstract

We introduce MoULDyS, that implements efficient offline and online monitoring algorithms of black-box cyber-physical systems w.r.t. safety properties. MoULDyS takes as input an uncertain log (with noisy and missing samples), as well as a bounding model in the form of an uncertain linear system; this latter model plays the role of an over-approximation so as to reduce the number of false alarms. MoULDyS is Python-based and available under the *GNU General Public License v3.0* (gpl-3.0). We further provide easy-to-use scripts to recreate the results of two case studies introduced in an earlier work.

*Keywords:* energy-aware monitoring, cyber-physical systems, formal methods, monitoring tool.

## **1** 1. Motivation and Significance

Monitoring consists of analyzing system logs, e.g., for detecting safety 2 violations (see, e.g., [4]). Monitoring has many useful applications such as 3 detecting the cause of a crash of vehicles. As an example, autonomous sys-4 tems are generally equipped with a device that records their state at periodic 5 or aperiodic time steps—logging the behavior of the system until the time 6 of a failure. A log, comprising of such recorded samples, is then investigated 7 for possible safety violations. Not only the logs can have samples missing at 8 various time steps, but also the recorded samples can have added noise to 9 it, e.g., due to sensor uncertainties. Analyzing such logs to detect possible 10 safety violations, that might have caused a failure, is known as offline mon-11 *itoring* when the analysis is done *a posteriori* (see, e.g., [5]). In contrast, it 12 is *online* when performed on-the-fly, when the whole log is not (yet) known 13 (see [6] for a discussion on online verification). 14

Preprint submitted to Science of Computer Programming

Nr.	Code metadata description	Please fill in this column
C1	Current code version	v1.1
C2	Permanent link to code/repository	https://github.com/bineet-coderep/MoULDyS/
	used for this code version	releases/tag/v1.1
C3	Permanent link to Reproducible	10.5281/zenodo.7888502
	Capsule	
C4	Legal Code License	GNU General Public License v3.0
		(gpl-3.0) [1]
C5	Code versioning system used	git
C6	Software code languages, tools, and	Python, numpy, scipy, mpmath,
	services used	pandas, Gurobi
C7	Compilation requirements, operat-	Provided in the installation
	ing environments and dependencies	guide $[2]$ .
C8	If available, link to developer docu-	Provided in the user guide [3].
	mentation/manual	
C9	Support email for questions	bineet@cs.unc.edu

Table 1: Code metadata

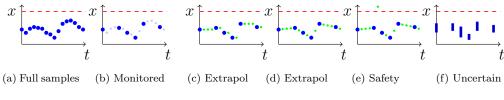


Figure 1: Monitoring at discrete time steps [9]

We introduce here MoULDyS<sup>1</sup> (see Table 1 for code metadata), a monitoring tool to analyze logs to detect possible safety violations. The specific features of MoULDyS are twofold: 1) the possibility to monitor aperiodic logs, or periodic logs with missing samples, and with possible noise over the recorded data; and 2) the presence of a bounding model following the formalism of uncertain linear systems.

Uncertain linear systems. Uncertain linear systems [7, 8] are a special subclass of non-linear systems that can be used to represent uncertainties and parameters in linear dynamical systems—for example, they can represent uncertain parameters in the cells of the dynamics matrix. Such a formalism is useful in representing an over-approximation of the model when the precise model is unknown or hard to obtain.

<sup>1</sup>https://sites.google.com/view/mouldys

Monitoring using uncertain linear systems as a bounding model. A challenge when performing offline monitoring is to "recreate" or guess the samples at 2 the missing time steps. That is, when the system under monitoring is a 3 black-box, with a log in the form of an aperiodic timed sequence of valuations of continuous variables (with missing valuations at various time steps): how to be certain that in between two discrete valuations the specification 6 was not violated at another discrete time step at which no logging was performed? Consider Fig. 1a, a system for which a logging occurs at every 8 discrete time step. When logging occurs at only *some* time steps (due to 9 some sensor faults, or to save energy with only a sparse, scattered logging), 10 a possible output is in Fig. 1b. In such a setting, how to be certain that, 11 in between two discrete samples, another discrete sample (not recorded) did 12 not violate the specification? That is, in Fig. 1b, there is no way to formally 13 guarantee that the unsafe zone (i.e., above the red, dashed line) was never 14 reached by another discrete sample which was not recorded. In many practical cases, a piecewise-constant or linear approximation (see, e.g., Figs. 1c 16 and 1d, where the large blue dots denote actual samples, while the small 17 green dots denote reconstructed samples using some extrapolation) is arbi-18 trary and not appropriate—it can yield a "safe" answer, while the actual 19 system could have actually been unsafe at some of the missing time steps. 20 On the contrary, assuming a completely arbitrary dynamics will always yield 21 "potentially unsafe"—thus removing the interest of monitoring. Without any 22 knowledge of the model, one can always assume that the behavior given in 23 Fig. 1e could happen. This behavior shows that the variable x is suddenly 24 crossing the unsafe region (dashed) at some unlogged discrete time step-25 even though this is unlikely if the dynamics is known to vary "not very fast". 26 To alleviate such issues, we proposed in [9] an offline monitoring algorithm us-27 ing a bounding model, i.e., a rough overapproximation of the system behavior 28 (originally introduced in [10] in a different context). The proposed method 29 is based on the reachable set computation of uncertain linear systems [11] 30 that can detect safety violations with limited false alarms.

We also considered in [9] an *online* monitoring algorithm, aiming at energetic efficiency, by recording samples only when required (i.e., when the system may get closer to a violation). MoULDyS implements both our offline and online monitoring algorithms [9]. We also provide here the steps to easily recreate the results of the two case studies in [9].

Experimental setting. Given an aperiodic (i.e., missing valuations at various time steps) and a noisy log (i.e., the valuations that are present in the log can have an added noise—an overapproximation of the actual state), MoULDyS can perform offline monitoring of the system to detect safety of the system behavior. Further, MoULDyS can be used in an online setting to log only when
necessary—thus targeting energy efficiency while logging. MoULDyS can be
run on a standard laptop with a Linux operating system (see the installation
guide for details [2]). The details of how to use the tool, with illustrative
examples, can be found in the user guide [3].

6 Outline. Section 2 describes the software; Section 3 describes the architec-7 ture; Section 4 describes the functionalities; Section 5 describes two illustra-8 tive examples from medical and automotive domains, with necessary steps 9 to recreate their results; Section 6 discusses the impact of MoULDyS; Sec-10 tion 7 briefly reviews related works; Section 8 concludes and discusses future 11 research.

## 12 2. Software Description

MoULDyS is an open-source software, implemented in Python, running on Linux platforms. Our experiments [9] suggest that MoULDyS is able to perform monitoring of reasonably large systems in a reasonable time. For example, we are able to monitor a five-dimensional system (i.e., a system with 5 continuous variables monitored at the same time) for 2000 time steps, with only actual 300 samples (note that, the fewer samples, the higher is the monitor computation time—as it is required to "recreate" the missing samples using reachable sets) in under 2.5 minutes on a standard laptop.

We believe that MoULDyS will not just be helpful to engineers to analyze logs to detect safety violations in several areas of research (such as in robotics to detect collision and other undesirable behaviors), but also to researchers to further develop monitoring-based approaches—in that case MoULDyS can be used for comparison.

#### 26 **3. Software Architecture**

The architecture of MoULDyS is given in Fig. 2. Each block in Fig. 2 rep-27 resents a core part (either functional or input) of the tool, and the arrows 28 indicate the flow of data. The dataflow of MoULDyS, for both Figs. 3 and 4 29 (offline and online monitoring respectively), starts from the blocks in the left 30 (e.g., bounding model, unsafe set, etc.) and ends at the extreme right of the 31 figures (outputting the safety status, visualization, and/or synthesized log). 32 Since both the offline (Block 1 of Figs. 2 and 3) and online monitoring algo-33 rithm (Block 2 in Figs. 2 and 4) uses reachability of uncertain linear systems 34 (Block 3 of Fig. 2), a data exchange occurs between Block 1 and Block 3, 35 as well as Block 2 and Block 3. MoULDyS implements a built-in reachability 36

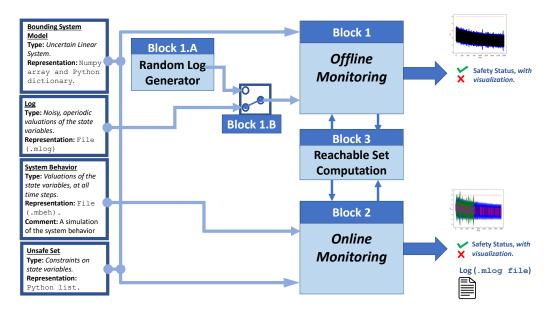


Figure 2: MoULDyS *Architecture*. Each block identifies a core part of the tool, and the arrows indicate the flow of data.

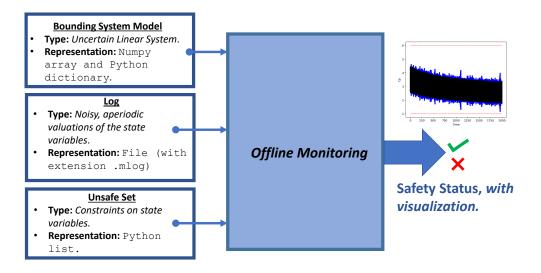


Figure 3: Dataflow diagram of the offline monitoring functionality of MoULDyS.

algorithm. The native reachable set computation support facilitates faster

computing (i.e., no data exchange with third party tool is required, which
 would potentially require additional data reformatting) with no additional

<sup>4</sup> tool installation required. MoULDyS employs an algorithm proposed in [11] to

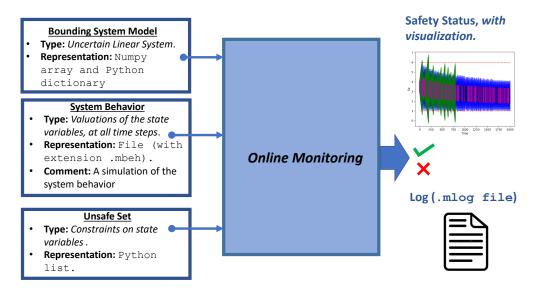


Figure 4: Dataflow diagram of the online monitoring functionality of MoULDyS.

compute the reachable set of uncertain linear systems. The algorithm first computes the reachable set of the nominal dynamics (which excludes uncer-2 tainties) and then computes the reachable set related to the uncertainties 3 in the dynamics. These two sets are then combined using the Minkowski 4 sum to obtain the reachable set of the entire dynamics. Although computing 5 the reachable set of the nominal dynamics is straightforward, the reachable set related to uncertainties is challenging to compute. After obtaining the 7 reachable sets, MoULDyS verifies the safety of these sets by comparing them 8 against provided safety specifications. These safety specifications are con-9 straints on state variables, which can be complex and involve multiple state 10 variables (e.g., linear inequalities involving several state variables). To rep-11 resent such safety specifications, MoULDyS uses a special type of polytope 12 called *zonotopes*, which can be expressed as an affine transformation of a 13 unit box. MoULDyS can check multiple safety specifications, each represented 14 as a zonotope and involving several state variables. 15

#### 16 3.1. Implementation

MoULDyS is implemented using Python 3.7.x, and runs in a Linux environment. The architecture is given in Fig. 2.

<sup>19</sup> The tool can be used in the following two ways. On the one hand, users

can use it through the provided virtual machine<sup>2</sup>, which already contains all the necessary dependencies and has the path variable set. Nevertheless, users 2 are still required to obtain and install the Gurobi license themselves, since 3 Gurobi only grants free academic licenses to individuals. On the other hand, 4 the tool can also be downloaded and setup from its public GitHub repository<sup>3</sup>. 5 If users aim to recreate the results in the paper or simply employ it for basic 6 monitoring purposes, using the provided virtual machine is recommended. 7 However, if the tool will be used for research and development purposes, it 8 is recommended to download and set it up on a local machine. The detailed 9 installation instructions are provided in [2]. The system model (represented 10 as an uncertain linear system), in MoULDyS, is represented with a numpy 11 array and a dictionary. The unsafe set is represented with a Python list. An 12 example code of how to encode the system model and its unsafe specification 13 can be found in the public repository<sup>4</sup>. The log and the system behavior, 14 on the other hand, is given as a file to MoULDyS (MoULDyS can also generate random logs; discussed later). Logs can either be represented as zonotopes 16 or intervals (an example of the required file can be found in MoULDyS public 17 repository<sup>5</sup>). 18

Both the online and offline monitoring algorithm (Block 1 and Block 2 of Fig. 2) have been implemented in Python using standard libraries, namely numpy, scipy and mpmath. The reachable set computation (Block 3 of Fig. 2) module implements the algorithm proposed in [11] in Python. Both the online and the offline module require performing intersection checking of zonotopes [9], which has been implemented as an optimization formulation using Gurobi. Gurobi has been further used to visualize the reachable sets.

Installation. While the virtual machine comes preinstalled with the required dependencies, setting up MoULDyS on a local machine requires installing the following dependencies: numpy, scipy, mpmath, pandas, Gurobi along with gurobipy (Gurobi requires an *ad-hoc* install but is free to use for academic purposes). The detailed steps for installing MoULDyS are given in the installation guide [2].

<sup>32</sup> User Guide. A tutorial on how to use several functionalities of MoULDyS, <sup>33</sup> along with sample codes (encoding a toy dynamics), is given in the user

<sup>&</sup>lt;sup>2</sup>10.5281/zenodo.7888502

<sup>&</sup>lt;sup>3</sup>https://github.com/bineet-coderep/MoULDyS/releases/tag/v1.1

<sup>&</sup>lt;sup>4</sup>https://www.github.com/bineet-coderep/MoULDyS/blob/main/src/tutorial/ TutorialOfflineMonitoring.py

<sup>&</sup>lt;sup>5</sup>https://www.github.com/bineet-coderep/MoULDyS/blob/main/data/toyEg\_5\_ interval.mlog

1 guide [3].

## 2 4. Software Functionalities

<sup>3</sup> In this section, we discuss the core functionalities of MoULDyS:

**Offline Monitoring** The offline monitoring requires the bounding model of the system (represented as an uncertain linear system) to be given as 5 input. Further, a log of the system behavior is required, which can be 6 achieved by the following ways: i) If the user already has a log to be monitored, it can be simply passed as an input to Block 1 of Fig. 2. 2 *ii*) Alternatively, MoULDyS can also generate a random (noisy and ape-0 riodic) log of the system, from a given initial set, using Block 1.A. The selection between the two possible choices is facilitated by Block 1.B. Analyzing the log, the final output of the offline monitoring is either safe (indicating the system behavior is certainly safe at all time steps), 13 or possibly-unsafe (indicating the system might have shown unsafe 14 behavior). An example code snippet to perform offline monitoring, on 15 a toy example, can be found in its public repository.<sup>6</sup>

**Online Monitoring** The online monitoring requires the bounding model of 17 the system (represented as an uncertain linear system) to be given as 18 input, as well as the actual behavior of the system. The actual behav-19 ior of the system is given as a file (with extension .mbeh) representing 20 the values of the state variables at every time step—an example of 21 the expected file (with extension .mbeh), containing valuation of the state variables at every time step, can be found in its public reposi-23 tory.<sup>7</sup> The final output of this feature is the safety status of the system 24 (safe/possibly-unsafe), and a synthesized log. An example code 25 snippet to perform online monitoring, on a toy example, can be found 26 in its public repository.<sup>8</sup>

As a side functionality, MoULDyS also allows to generate random logs (using Block 1.A). While this is not strictly speaking part of monitoring, it greatly helps to perform experiments using MoULDyS. Basically, given a

<sup>&</sup>lt;sup>6</sup>https://www.github.com/bineet-coderep/MoULDyS/blob/main/src/tutorial/ TutorialOfflineMonitoring.py

<sup>&</sup>lt;sup>7</sup>https://www.github.com/bineet-coderep/MoULDyS/blob/main/data/toyEg\_5\_ interval.mbeh

<sup>&</sup>lt;sup>8</sup>https://www.github.com/bineet-coderep/MoULDyS/blob/main/src/tutorial/ TutorialOnlineMonitoring.py

bounding model, MoULDyS can generate a random log following the bounding
 model.

### **5.** Illustrative examples

In this section, we briefly recall the two case studies presented in [9] that use a prototype version of MoULDyS. The two case studies, automated anesthesia delivery and adaptive cruise control, demonstrate the applicability and usability of MoULDyS. Further, we provide detailed steps to recreate the results presented in [9] using MoULDyS.

**Anesthesia** [12] presents an automated anaesthesia delivery model, with 9 the drug propofol. The system models the metabolization of the drug by the body, and the depth of hypnosis. The state variables encode 11 the various concentration levels—that must be within a certain limit 12 at all times—modeling the metabolization of the drug and the depth of 13 hypnosis. Note that a higher concentration level would mean that the 14 patient remains unconscious for a longer period of time, while a lower concentration level would mean that patient remains conscious during 16 the surgery—which can be traumatic. MoULDyS can help performing an 17 automated monitoring of the patients without compromising on safety. 18

Adaptive Cruise Control (ACC) [13] presents a model of ACC with 19 state variables as velocity, distance between two vehicles, and the ve-20 locity of the lead vehicle. Offline monitoring provides an automated 21 way to detect the *cause of the crash* and *who was at fault*. Similarly, consider a vehicle driving on a highway with a vehicle in its sight. The 23 ACC unit will have to continuously read sensor values to track sev-24 eral parameters, such as acceleration of the lead vehicle, braking force, 25 etc.—causing a waste of energy. In these cases, deploying online mon-26 itoring on the vehicle ACC will ensure that the sensor values are only 27 read when there is a potential unsafe behavior—thus saving energy. 28 [9] provides several such practical cases where monitoring is useful—in 29 [9, Figs. 5 and 6] (also recalled in the appendix in Figs. B.8 and B.9 30 respectively). 31

The case studies mentioned above study the following aspects with regards to monitoring: *i*) Impact of number of samples in the log. *ii*) Impact of uncertainties in the samples of the log. *iii*) Demonstrating online monitoring. *iv*) Comparing offline and online monitoring. In the following, we provide the detailed steps to recreate the results in [9, Section 5]. In particular, the results that we wish to recreate, from [9], are given in Figs. B.6 to B.9.

#### <sup>1</sup> 5.1. Recreating Results

The results of the Anesthesia case study and the ACC case study can be recreated by using the scripts provided in the GitHub repository<sup>9</sup>. The detailed steps to recreate the results from both the case studies are given in [14].

Note that, in [9, Section 5], logs were randomly generated *during our experiments*, and therefore the results from [9, Section 5] cannot be *stricto sensu* be recreated, as their reproducibility script re-generates a random log, which may differ from the one actually shown in [9, Section 5].

Therefore, we modified our scripts so that the log is given as an input, on which monitoring is performed: we thus generated the logs statically, and embedded them in the reproducibility capsule, in order for users to reproduce exactly the result we present here. These logs were generated with the same logging probabilities (and initial sets) as in [9, Section 5]. In the rest of the section, we discuss the steps for replicating the new Figs. B.6 to B.9.

Anesthesia. The main results of the Anesthesia case study are pro-16 vided in Figs. B.6 and B.7 (variant of [9, Figures 3 and 4]). We 17 use python Anesthesia.py -offline i, with i  $\in \{1, 2, 3, 4\}$  to recre-18 ate Figs. B.6a to B.6d respectively. To recreate Fig. B.7a, we 19 use python Anesthesia.py -online. To recreate Fig. B.7b, we use 20 python Anesthesia.py -compare. The Anesthesia.py script is provided in its GitHub repository.<sup>10</sup> 22

ACC. The main results of the ACC case study are provided in Figs. B.8
and B.9 (variant of [9, Figures 5 and 6]). The results of the ACC case study
can be recreated in a similar manner to the Anesthesia case study, by simply
using the ACC.py<sup>11</sup> script instead of the Anesthesia.py script.

## 27 6. Impact

While MoULDyS remains a prototype based on a recent algorithm [9], and is by no means a widely used software in an industrial context for the time being, we believe it has an interesting potential to gain up a user base interested in monitoring black-box cyber-physical systems against safety properties. To the best of our knowledge, it is the first software allowing monitoring logs

<sup>&</sup>lt;sup>9</sup>https://www.github.com/bineet-coderep/MoULDyS/tree/main/src/recreate\_results\_from\_paper <sup>10</sup>https://www.github.com/bineet-coderep/MoULDyS/blob/main/src/recreate\_results\_from\_ paper/Aposthesia\_py

paper/Anesthesia.py
 <sup>11</sup>https://github.com/bineet-coderep/MoULDyS/blob/main/src/recreate\_results\_from\_paper/
ACC.py

featuring not only uncertainty (due to sensor's imperfect behavior) but also
potentially missing samples, together with a bounding model going beyond
the class of linear systems. This is in contrast with, e.g., [10] in which our
bounding model was restricted to linear models.

In addition, MoULDyS can perform *online* monitoring, with a focus on energetic efficiency: by triggering a sample recording only when necessary (i.e., when MoULDyS informs the system that it may get close to an unsafe behavior according to its online algorithm), the system saves energy, i.e., only records samples (which needs network bandwidth usage, as well as processor and memory usage) when necessary instead of at every time unit.

Our applications recalled in Section 5 show that MoULDyS can be applied to challenging domains such as health and autonomous driving, giving interesting results (e.g., limited number of false alarms) in a reasonable execution time making it suitable to real-time applications.

### <sup>15</sup> 7. Related works

Monitoring complex systems, and notably cyber-physical systems, drew a lot of attention in the last decades [4]. We briefly review close works in the following.

MONPOLY [15] is a monitoring tool taking as specification formulas expressed using MFOTL (metric first-order temporal logic). It is entirely black-box: the only input beyond the formula is the *log*, i.e., a sequence of timestamped system events, potentially with numeric arguments (e.g., "@10 withdraw (Alice,6000)", expressing that a withdrawal occurs at timestamp 10).

In [16], the focus is on online monitoring over real-valued signals, using MTL as the specification formalism. Again, the system is black-box.

In [17], parametric timed pattern matching is made, on an entirely blackbox system, i.e., without any prior knowledge of the system; the tools used are IMITATOR [18] and a prototypal tool ParamMONAA. The output is a set of intervals where a property is valid/violated, possibly with a set of timing parameter valuations.

In [10], we proposed *model-bounded monitoring*: instead of monitoring a black-box system against a sole specification, we use in addition a (limited, over-approximated) knowledge of the system, to eliminate false positives. This over-approximated knowledge is given in [10] in the form of a *linear hybrid automaton* (LHA) [19]. We use in [10] both an *ad-hoc* implementation, and another one based on PHAVerLite [20]. In this work, we share with [10] the principle of using an over-approximation of the model to rule out some

violation of the specification, which comes in contrast with the aforemen-1 tioned works. However, we consider here a different formalism, and we work 2 on discrete samples. In terms of expressiveness of the over-approximated 3 model, while our approach can be seen as less expressive than [10], in the sense that we have a single (uncertain) dynamics (as opposed to LHAs, where 5 a different dynamics can be defined in each mode), our dynamics is also sig-6 nificantly more expressive than the LHA dynamics of [10]; we consider not 7 only the class of linear dynamical systems, but even fit into a special case of 8 non-linear systems, by allowing *uncertainty* in the model dynamics. 9

In [21, 22], a monitor is constructed from a system model in differential dynamic logic [23]. The main difference between [21, 22] and our approach relies in the system model: in [21, 22], the compliance between the model and the behavior is checked at runtime, while our model is assumed to be an over-approximation of the behavior—which is by assumption compliant with the model.

#### 16 8. Conclusion and Future Work

Monitoring black-box complex cyber-physical systems can be delicate, 17 and may lead to false alarms. MoULDyS is a Python-based tool implementing 18 offline and online monitoring algorithms. A first crux of MoULDyS is to be able 19 to manage logs with uncertainty over the logged state variables, as well as 20 missing samples. A second crux is the use of a bounding model in the form 21 of uncertain linear systems, helping to reduce the number of false alarms. 22 MoULDyS can analyze logs efficiently to detect possible safety violations that 23 might have caused an unsafe behavior. Further, MoULDyS can also be used 24 in an online setting where the system is sampled only when there is a risk 25 of safety violation. As a result, the online monitoring is able to decrease 26 the number of samples, therefore reducing energy consumption at runtime. 27 MoULDyS is available under the GNU General Public License. 28

In future, we wish to extend MoULDyS to support uncertainty not only in the log valuations (the value of a sensor at a given timestamp), but also uncertainty in the log timestamps themselves: this makes sense when some sensors are distributed with drifting clocks, or when network delays make the exact recording timestamp imprecise.

#### 34 Acknowledgements (optional)

Bineet Ghosh was supported by the National Science Foundation (NSF) of the United States of America under grant number 2038960. This work is partially supported by the ANR-NRF French-Singaporean research program ProMiS (ANR-19-CE25-0015 / 2019 ANR NRF 0092) and by ANR BisoUS
 (ANR-22-CE48-0012).

# **3 References**

- [1] GNU General Public License v3.0, https://www.gnu.org/licenses/
   gpl-3.0.en.html.
- [2] MoULDyS installation guide, https://www.github.com/
   bineet-coderep/MoULDyS/blob/main/documentation/
   installation\_guide.md (2022).
- [3] MoULDyS user guide, https://www.github.com/bineet-coderep/
   MoULDyS/blob/main/documentation/user\_guide.pdf (2022).
- [4] E. Bartocci, J. V. Deshmukh, A. Donzé, G. E. Fainekos, O. Maler,
  D. Ničković, S. Sankaranarayanan, Specification-based monitoring of
  cyber-physical systems: A survey on theory, tools and applications,
  in: E. Bartocci, Y. Falcone (Eds.), Lectures on Runtime Verification
  Introductory and Advanced Topics, Vol. 10457 of Lecture Notes
  in Computer Science, Springer, 2018, pp. 135–175. doi:10.1007/
  978-3-319-75632-5\_5.
- [5] D. A. Basin, G. Caronni, S. Ereth, M. Harvan, F. Klaedtke, H. Mantel, Scalable offline monitoring of temporal specifications, Formal Methods in System Design 49 (1-2) (2016) 75–108. doi:10.1007/s10703-016-0242-y.
- [6] O. Maler, Some thoughts on runtime verification, in: Y. Falcone,
   C. Sánchez (Eds.), RV, Vol. 10012 of Lecture Notes in Computer Science,
   Springer, 2016, pp. 3–14. doi:10.1007/978-3-319-46982-9\_1.
- [7] R. Lal, P. Prabhakar, Bounded error flowpipe computation of parameterized linear systems, in: A. Girault, N. Guan (Eds.), EMSOFT, IEEE,
   2015, pp. 237–246. doi:10.1109/EMSOFT.2015.7318279.
- [8] B. Ghosh, P. S. Duggirala, Robust reachable set: Accounting for uncertainties in linear dynamical systems, ACM Transactions on Embedded
   Computing Systems 18 (5s) (2019) 97:1–97:22. doi:10.1145/3358229.
- [9] B. Ghosh, E. André, Monitoring of scattered uncertain logs using uncertain linear dynamical systems, in: M. Mousavi, A. Philippou (Eds.),
   FORTE, Vol. 13273 of Lecture Notes in Computer Science, Springer,
   2022, pp. 67–87. doi:10.1007/978-3-031-08679-3\_5.

- [10] M. Waga, É. André, I. Hasuo, Model-bounded monitoring of hybrid systems, ACM Transactions on Cyber-Physical Systems 6 (4) (2022) 30:1–30:26. doi:10.1145/3529095.
- [11] B. Ghosh, P. S. Duggirala, Robustness of safety for linear dynamical systems: Symbolic and numerical approaches, Tech. Rep. 2109.07632, arXiv (2021).
- [12] V. Gan, G. A. Dumont, I. Mitchell, Benchmark problem: A PK/PD
  model and safety constraints for anesthesia delivery, in: G. Frehse,
  M. Althoff (Eds.), ARCH@CPSWeek, Vol. 34 of EPiC Series in Computing, EasyChair, 2014, pp. 1–8. doi:10.29007/8drm.
- [13] P. Nilsson, O. Hussien, A. Balkan, Y. Chen, A. D. Ames, J. W. Grizzle,
   N. Ozay, H. Peng, P. Tabuada, Correct-by-construction adaptive cruise
   control: Two approaches, IEEE Transactions on Control Systems Technology 24 (4) (2016) 1294–1307. doi:10.1109/TCST.2015.2501351.
- 15 [14] MoULDyS: Recreating results, https://www.github.com/ 16 bineet-coderep/MoULDyS/blob/main/documentation/recreate\_ 17 results.md (2022).
- [15] D. A. Basin, F. Klaedtke, E. Zalinescu, The MonPoly monitoring tool,
  in: G. Reger, K. Havelund (Eds.), RV-CuBES, Vol. 3 of Kalpa Publications in Computing, EasyChair, 2017, pp. 19–28.
- [16] K. Mamouras, A. Chattopadhyay, Z. Wang, A compositional framework for quantitative online monitoring over continuous-time signals,
  in: L. Feng, D. Fisman (Eds.), RV, Vol. 12974 of Lecture Notes
  in Computer Science, Springer, 2021, pp. 142–163. doi:10.1007/
  978-3-030-88494-9\_8.
- [17] M. Waga, É. André, I. Hasuo, Parametric timed pattern matching, ACM
   Transactions on Software Engineering and Methodology 32 (1) (2022)
   10:1–10:35. doi:10.1145/3517194.
- [18] É. André, IMITATOR 3: Synthesis of timing parameters beyond decidability, in: R. Leino, A. Silva (Eds.), CAV, Vol. 12759 of Lecture Notes in Computer Science, Springer, 2021, pp. 1–14. doi:10.1007/ 978-3-030-81685-8\_26.
- [19] N. Halbwachs, Y.-É. Proy, P. Raymond, Verification of linear hybrid
   systems by means of convex approximations, in: B. Le Charlier (Ed.),



Figure A.5: MoULDyS Logo.

1	SAS, Vol. 864 of Lecture Notes in Computer Science, Springer, 1994,
2	pp. 223-237. doi:10.1007/3-540-58485-4_43.

- [20] A. Becchi, E. Zaffanella, Revisiting polyhedral analysis for hybrid
   systems, in: B. E. Chang (Ed.), SAS, Vol. 11822 of Lecture Notes
   in Computer Science, Springer, 2019, pp. 183–202. doi:10.1007/
   978-3-030-32304-2\_10.
- [21] S. Mitsch, A. Platzer, ModelPlex: verified runtime validation of verified
   cyber-physical system models, Formal Methods in System Design 49 (1 (2016) 33-74. doi:10.1007/s10703-016-0241-z.
- [22] S. Mitsch, A. Platzer, Verified runtime validation for partially observable
   hybrid systems, Tech. rep. (2018). arXiv:1811.06502.
   URL http://arxiv.org/abs/1811.06502
- [23] A. Platzer, The complete proof theory of hybrid systems, in: LICS, IEEE
   Computer Society, 2012, pp. 541–550. doi:10.1109/LICS.2012.64.

# 15 Appendix A. MoULDyS: A Monitoring Tool for Autonomous Systems

- <sup>16</sup> The various details of MoULDyS are given as follows:
- <sup>17</sup> Logo The tool logo is given in Fig. A.5.
- Webpage The tool webpage can be found here: https://www.sites.
   google.com/view/mouldys.

Code MoULDyS is an open-source tool under the gpl-3.0 license. The
 code can be found in a public GitHub repository: https://github.com/
 bineet-coderep/MoULDyS/releases/tag/v1.1.

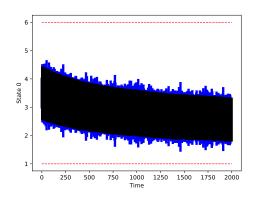
<sup>4</sup> Installation Guide The installation guide is available in [2].

<sup>5</sup> User Guide The user guide is available in [3].

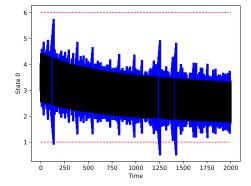
Result Recreation Guide Guide A prototype version of MoULDyS was
 used to perform the experiments in [9]. The detailed steps to recreate the results in [9], through easy-to-use scripts, are available in [14].

## 9 Appendix B. Recreating Experimental Results

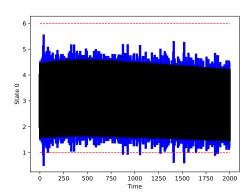
The results to be recreated for the Anesthesia case study are given in Figs. B.6 and B.7. The results to be recreated for the ACC case study are given in Figs. B.8 and B.9.



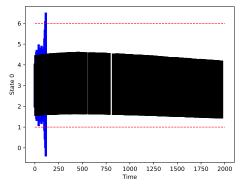
(a) Monitoring with frequent samples, and low uncertainty



(c) Monitoring with sporadic samples, and low uncertainty



(b) Monitoring with frequent samples, and high uncertainty



(d) Monitoring with sporadic samples, and high uncertainty

Figure B.6: Offline Monitoring (Anesthesia). We plot the change in concentration level of  $c_p$  with time. The volume of the samples increases from left to right, and the probability of logging increases from bottom to top. The blue regions are the reachable sets showing the over-approximate reachable sets as computed by the offline monitoring, the black regions are the samples from the log given to the offline monitoring algorithm, and the red dotted line represents safe distance level. Note that although Figure 1 and Figure 4 (Figs. B.6b and B.6c) reachable sets' seem to intersect with the red line (unsafe set), the refinement module infers them to be unreachable, therefore concluding the system behavior as safe—unlike Fig. B.6d. These plots are a stochastic recreation of [9, Figure 3].

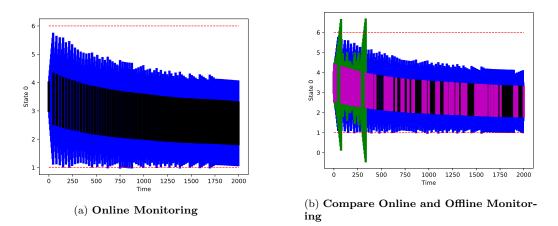
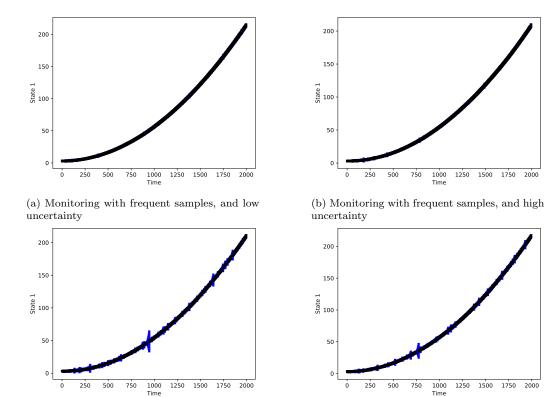


Figure B.7: Online Monitoring (Anesthesia). We plot the change in concentration level of  $c_p$  with time. The blue regions are the reachable sets showing the over-approximate reachable sets as computed by the online monitoring, the black regions are the samples generated when the logging system was triggered by the online monitoring algorithm, and the red dotted line represents safe concentration levels. Online Monitoring (Fig. B.7a): We apply our online monitoring to the anesthesia model. Compare (Fig. B.7b): We compare our online and offline algorithms. The green regions are the reachable sets showing the over-approximate reachable sets between two consecutive samples from the offline logs, the magenta regions are the offline logs, given as an input to the offline monitoring algorithm, generated by the logging system, and the red dotted line represents safe concentration levels. The blue regions are the reachable sets showing the over-approximate reachable sets as computed by the online monitoring, the black regions are the samples generated when the logging system was triggered by the online monitoring algorithm, and the red dotted line represents safe concentration levels. These plots are a stochastic recreation of [9, Figure 4].



(c) Monitoring with sporadic samples, and low uncertainty

(d) Monitoring with sporadic samples, and high uncertainty

Figure B.8: **Offline Monitoring (ACC).** We plot the change in distance h between the vehicles with time. The volume of the samples increases from left to right, and the probability of logging increases from bottom to top. These plots are a stochastic recreation of [9, Figure 5]

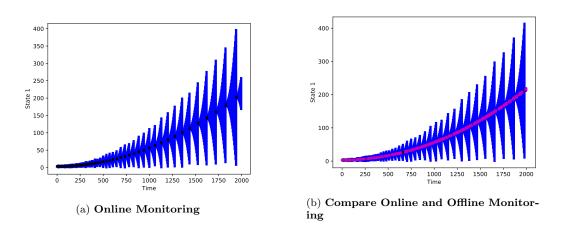


Figure B.9: Online Monitoring (ACC). We plot the change in distance between two vehicle h with time. The color coding is same as Fig. B.7. Online Monitoring (Fig. B.9a): We apply our online monitoring to the ACC model. Compare (Fig. B.9b): We compare our online and offline algorithms. These plots are a stochastic recreation of [9, Figure 6]